

# LONG-RANGE BEAM-BEAM EXPERIMENTS IN THE RELATIVISTIC HEAVY ION COLLIDER

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## Abstract

Long-range beam-beam effects are a potential limit to the LHC performance with the nominal design parameters, and certain upgrade scenarios under discussion. To mitigate long-range effects, current carrying wires parallel to the beam were proposed and space is reserved in the LHC for such wires. Two current carrying wires were installed in RHIC to study the effect of strong long-range beam-beam effects in a collider, as well as test the compensation of a single long-range interaction. The experimental data were used to benchmark simulations. We summarize this work.

## INTRODUCTION

The reader should note that this is an identical copy of an article first published in [1]. Beam-beam effects have limited the performance of previous and existing hadron colliders [2–4] such as the ISR [5, 6], Sp̄pS [7–10], Tevatron [11–13] and RHIC [14, 15], and are also expected to limit the performance of the LHC [16–31].

Beam-beam effects can be categorized as either incoherent (dynamic aperture and beam lifetime), PACMAN (bunch-to-bunch variations), or coherent (beam oscillations and instabilities) [25]. These effects can be caused by both head-on and long-range interactions. Head-on effects, leading to tune shifts and spreads, are important in all hadron colliders. Total beam-beam induced tune shifts as large as 0.028 were achieved in the Sp̄pS [10] and Tevatron [13], although operational tune shift values are somewhat lower. The LHC in its early stages of commissioning has already reached a total head-on beam-beam tune shift of 0.02 [32].

Long-range effects, however, differ in previous and existing colliders. In the ISR the beams collided under a large crossing angle of 15 deg [33] that greatly reduced long-range effects. In the Sp̄pS, with both beams in the same aperture and only three bunches per beam, there were a few long-range interactions distributed over the ring circumference. Due to the difference in the bunch intensities, the effect on the anti-protons was stronger. In the Tevatron, also with both beams in the same aperture but 36 bunches per beam, there are more long-range interactions. With increased intensity of the anti-proton bunches, protons can also be affected.

In RHIC (Fig. 1), where both beams share the same aperture only in the interaction regions, there is only one long-range interaction per interaction region without an experiment (a total of four in the current configuration), with a

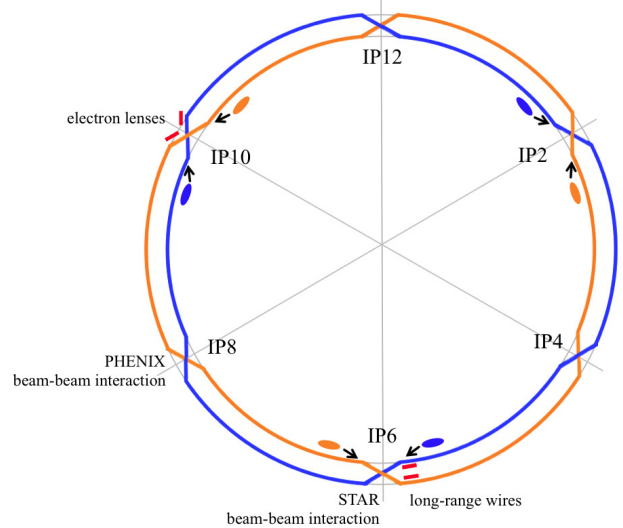


Figure 1: Beam-beam interactions in RHIC and locations of wires and electron lenses.

10 mm separation (corresponding to 30 rms beam sizes for protons at 250 GeV energy). Long-range interactions have affected the RHIC ramp transmission in the past [14].

## LONG-RANGE EFFECTS AND COMPENSATION IN THE LHC

In the LHC there are 32 long-range beam-beam interactions localized in each of four interaction regions [25]. A major upgrade of the LHC interactions region is foreseen by the end of the decade with the primary objective to increase the average luminosity of the machine by about a factor of 5 to 10 above the design performance. Among the various upgrade scenarios a crab crossing scheme (CC), an early beam separation scheme (ES), and a large Piwinski angle (LPA) are considered. In the CC scheme, crab cavities placed on either side of the interaction region impart a transverse kick to effectively compensate the crossing angle. This scheme allows for a large crossing angle that greatly reduces long-range beam-beam effects. In the ES scheme [27, 28] the number of long-range interactions is greatly reduced but four parasitic collisions at 4–5  $\sigma$  per IP remain. In the LPA scheme [26] the small crossing angle will be maintained, and long bunches of intensities up to  $4\text{--}5 \times 10^{11}$  protons are used. All schemes aim at higher than nominal bunch currents and reduced  $\beta^*$ . Therefore, long-range effects tend to become more problematic and require

more aperture for larger crossing angles or compensation to mitigate these effects. The LPA scheme would most benefit from long-range beam–beam compensation. The compensation of long-range effects in the Tevatron was proposed with electron lenses [34], and in the LHC with wires [35]. Electron lenses were also considered for the LHC [36], and the use of wires was also studied for the Tevatron [37]. Implementation of long-range beam–beam compensation in the Tevatron is challenging because the effect is distributed over the whole ring. In the LHC the effect is localized in the interaction regions. A partial long-range beam–beam compensation was successfully implemented in the  $e^+e^-$  collider DAΦNE [38]. Beam–beam compensation and related issues were reviewed at a workshop in 2007 [39].

## RHIC AS A TEST BENCH FOR LONG-RANGE STUDIES

Figures 1 and 2 show the basic layout of the beam–beam interaction and compensation studies in RHIC. At store there are nominally two head-on interactions in points 6 and 8 (IP6 and IP8), and long-range interactions with a large separation in the other interaction points. Three bunches in the Blue ring are coupled to three bunches in the Yellow ring through the head-on beam–beam interaction. For studies, two DC wires were installed in the Blue and Yellow rings respectively in interaction region 6 (IR6). Table 1 shows the main beam parameters for polarized proton operation, both achieved and design. In RHIC the beam–beam effect is strongest in proton operation.

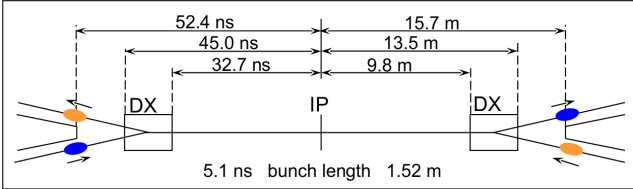


Figure 2: Schematic of the RHIC interaction regions.

Table 1: Main RHIC parameters achieved in polarized proton operation that are relevant for beam–beam effects protons (2009). Note that the polarized proton bunch intensity is also limited by intensity dependent depolarization effects in the AGS.

Quantity	Unit		
Beam energy, $E_b$	GeV	100	250
Bunch intensity, $N_b$	$10^{11}$	1.35	1.1
Norm emittance, $\epsilon$	$\mu\text{m}$	2.5	3.0
rms bunch length, $\sigma_z$	m	0.85	0.60
Beam–beam parameter $\xi/\text{IP}$	...	0.0056	0.0045
No of IPs	...	2	2
$\beta^*$ at IP6, IP8	m	0.7	0.7

In the LHC locations in warm sections of the interaction regions are reserved to accommodate long-range beam–beam wire compensators (Fig. 3), or electron lenses.

These locations have about equal horizontal and vertical  $\beta$ -functions. With the expected strong long-range beam–beam effects in the LHC, and the proposed wire compensation, experimental data and simulations of long-range effects are highly desirable. Operational and experimental data exist from the Sp̄pS and the Tevatron. In the SPS, wires were installed to further investigate strong long-range beam–beam interactions, to test the compensation scheme, and to benchmark simulations [30, 40–42].

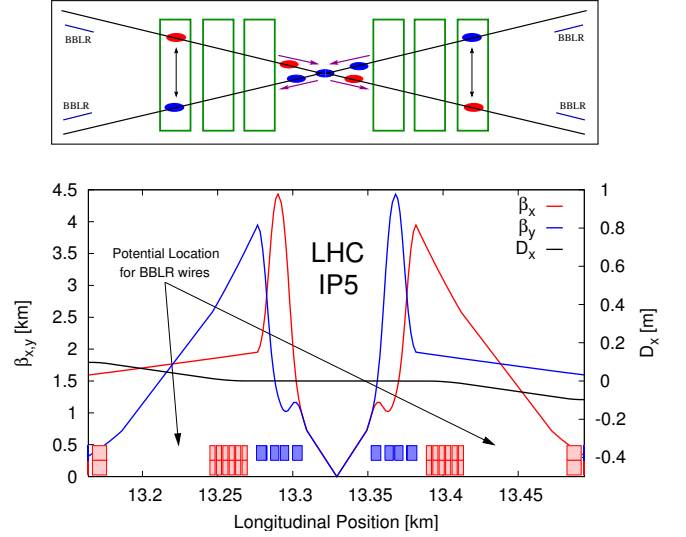


Figure 3: LHC interaction region schematically showing the common focusing channel with the 32 long-range interactions on the left and the right of the collision point (top) and the optics functions in the region.

The wire experiments in RHIC complement these studies. The beam lifetime in RHIC is typical for a collider and better than in the SPS wire experiments. In addition, and unlike in the SPS, head-on effects can be included, and with properly placed long-range interactions and wires, the compensation of a single long-range interaction is possible.

## WIRES IN RHIC

The RHIC wire design is based on experience gained with the SPS units. Design considerations are: the location in ring, the integrated strength ( $IL$ ), the wire temperature  $T$  in operation, the positioning range and accuracy, power supply requirements, controls, and diagnostics [43, 44]. The wire parameters are shown in Table 2.

### Location in the Ring

For a successful compensation the phase advance between the long-range interaction and the compensator should be no larger than about 10 degrees [45]. Lattices with  $\beta^* \leq 1.0$  m have such small phase advances between the entrance to the DX and the exit of Q3. Thus it is possible to place a wire in the warm region after Q3 to compensate for a long-range beam–beam interaction near the DX

Table 2: Parameters for RHIC wires. The wire material is Cu at 20°C. The nominal wire strength is for a single long-range interaction with a proton bunch intensity of  $2 \times 10^{11}$ .

Quantity	Unit	Value
Strength ( $IL$ ), nominal	A m	9.6
Max. strength ( $IL$ ) <sub>max</sub>	A m	125
Length of wire $L$	m	2.5
Radius of wire $r$	mm	3.5
Number of heat sinks $n$	...	3
Electrical resistivity $\rho_e$	$\Omega$ m	$1.72 \times 10^{-8}$
Heat conductivity $\lambda$	$W m^{-1} K^{-1}$	384
Thermal expansion coeff.	$K^{-1}$	$1.68 \times 10^{-5}$
Radius of existing pipe $r_p$	mm	60
Current $I$ , nominal	A	3.8
Max. current $I_{max}$	A	50
Current ripple $\Delta I/I$ (at 50 A)	$10^{-4}$	$< 1.7$
Electric resistance $R$	m $\Omega$	1.12
Max. voltage $U_{max}$	mV	55.9
Max. power $P_{max}$	W	2.8
Max. temp. change $\Delta T_{max}$	K	15
Max. length change $\Delta L_{max}$	mm	0.4
Vertical position range	mm/ $\sigma_y$	65/10.6

magnet (Fig. 4). Since the beam paths must cross horizontally, it is easier to control the distance between the beams in an experiment through vertical separation. To compensate for a vertical long-range interaction near the DX magnet, one wire can be installed in each ring (see Fig. 5). In the Blue ring the wire is installed below the beam axis, in the Yellow ring above the beam axis.

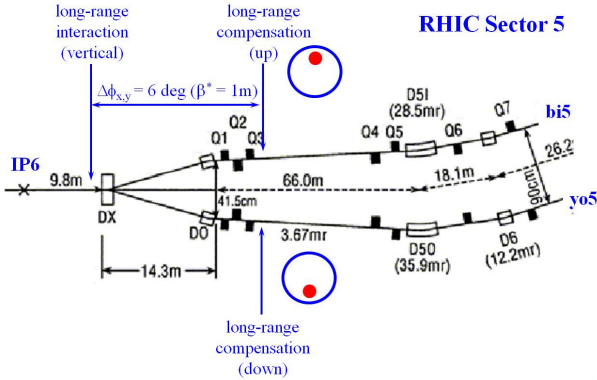


Figure 4: Location of wires in RHIC and location of long-range beam-beam interaction for compensation.

### Integrated Strength

To compensate a single long-range interaction, the compensator's integrated strength ( $IL$ ) must be the same as the opposing bunch's current integrated over its length ( $IL$ ) =  $N_b e c$ , where  $I$  is the current in the wire,  $L$  its length,  $N_b$  the bunch intensity,  $e$  the elementary charge, and  $c$  the speed of light (see Table. 2).

In the LHC, an integrated strength of 80 A m is required to correct for the 16 long-range interactions on either side

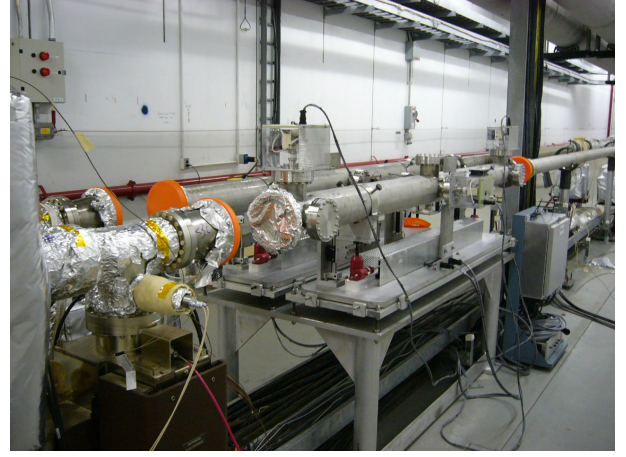


Figure 5: The two long-range beam-beam wires in the RHIC tunnel during installation.

of an IR [35]. Such a strength is also expected to lead to enhanced diffusion at amplitudes larger than 6 rms transverse beam sizes [45]. To study the enhanced diffusion in RHIC, the wire is designed for  $(IL)_{max} = 125$  A m.

### Wire Temperature

The wire temperature should not exceed 100°C to avoid increased outgassing of the vacuum components. We use a number of air cooled heat sinks to limit the wire temperature.

Assume first a wire in vacuum of radius  $r$  and length  $l$ , with electrical resistivity  $\rho_e$  and heat conductivity  $\lambda$ . A current  $I$  flows through the wire, and at both ends there are heat sinks that maintain the temperature  $T_0$ . Further we assume that the temperature rise  $\Delta T$  in the wire is small enough so that the material coefficients  $\rho_e$  and  $\lambda$  are constants. In each length element  $dx$  heat  $dQ$  is produced through the wire's resistivity at the rate

$$\frac{dQ}{dt} = \rho_e \frac{dx}{\pi r^2} I^2, \quad (1)$$

and the heat flow is connected to the temperature gradient  $dT(x)/dx$  via the heat equation

$$\frac{dQ}{dt} = -\lambda \pi r^2 \frac{dT}{dx}. \quad (2)$$

Combining Eqs. (1) and (2) yields the differential equation for the temperature

$$\frac{dT^2(x)}{dx^2} = -\frac{\rho_e}{\lambda} \frac{I^2}{\pi^2 r^4} \quad (3)$$

with the solution

$$T(x) = -\frac{1}{2\pi^2} \frac{\rho_e}{\lambda} \frac{I^2}{r^4} x^2 + ax + b. \quad (4)$$

The coefficients  $a$  and  $b$  can be determined from the boundary conditions  $T(0) = T(l) = T_0$  yielding

$$T(x) = T_0 + \frac{1}{2\pi^2} \frac{\rho_e}{\lambda} \frac{I^2}{r^4} (xl - x^2). \quad (5)$$

The maximum temperature increase  $\Delta T_{\max}$  is in the centre of the wire,  $x = l/2$ , and is

$$\Delta T_{\max} = \frac{1}{8\pi^2} \frac{\rho_e}{\lambda} \frac{(Il)^2}{r^4}. \quad (6)$$

If we now assume a wire of length  $L$  with  $n$  heat sinks, we can replace  $l$  by  $L/(n-1)$  in Eq. (6) and arrive at

$$\Delta T_{\max} = \frac{1}{8\pi^2} \frac{\rho_e}{\lambda} \frac{(IL)^2}{(n-1)^2 r^4}. \quad (7)$$

We use  $n = 3$  heat sinks cooled with forced air. To move the wire compensator close to the beam, its radius should not be much larger than an rms transverse beam size. The calculated temperature change is shown in Table 2. Figure 6 shows a drawing of the end of a wire. Visible are the wire support, the electrical feed-through which is also a heat sink, and a connecting loop allowing for thermal expansion of the wire.

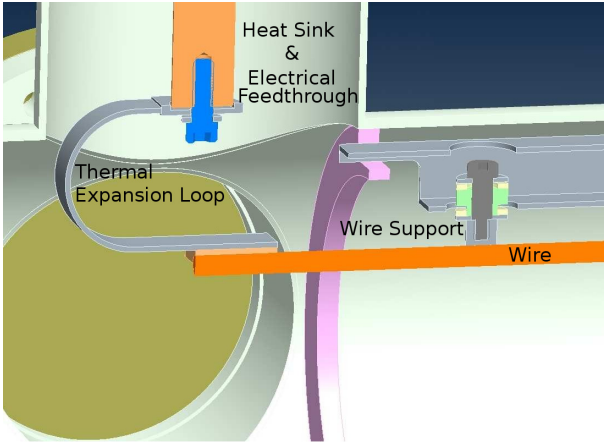


Figure 6: Drawing of the end of a long-range beam–beam wire in RHIC.

### Power Supply Requirements

To limit emittance growth, a current ripple of  $\Delta I/I < 10^{-4}$  is required [45]. A measurement shows a current ripple of  $\Delta I/I < 1.7 \times 10^{-4}$  where the upper limit is given by the noise floor of the current measurement.

## LONG-RANGE EXPERIMENTS AT RHIC

More than 30 dedicated Long-Range (LR) beam–beam experiments were performed at different energies, with different species and various machine configurations. They span a variety of long-range conditions which help benchmark simulation tools. The main parameters that were varied were the strength of the long-range interactions (wire current), the distance between the beam and the wire (or other beam), the tune and chromaticity. All experimental sessions to study long-range beam–beam interactions in RHIC can be broadly classified into three categories approximately in chronological order:

- measurement of a single long-range interaction between the two proton bunches at 23 and 100 GeV in IP6;
- effect of the DC wires on a single beam either by varying the current at a fixed distance or varying the distance to the beam with fixed current on both protons at 100 GeV and gold at 100 GeV/nucleon;
- effect of long-range interaction either with a wire in the presence of head-on collisions or long-range interactions between the two beams in IP6 with simultaneous compensation using a wire at 100 GeV.

A summary of all long-range experiments performed in the RHIC accelerator between 2005 to 2009 is listed with corresponding beam conditions in Table 3. The main observables in long-range beam–beam experiments are orbits, tunes, Beam Transfer Functions (BTFs), and the beam lifetime. Several simulations were performed for a subset of measurements which show successful reconstruction of all measurable quantities and the onset of losses [46]. Specific examples for each of the three categories with detailed results are presented in the next sections to summarize all the long-range experiments performed at RHIC.

### Single Long-range Measurements

The first set of long-range beam–beam experiments were performed with proton beams in 2006. The motivation of these experiments was to characterize the effect of one parasitic interaction on beam losses for a future compensation demonstration. The Blue and Yellow beams were vertically separated in the IR6 region close to the DX magnet (Fig. 2). The RHIC beams are very stable at the nominal working point and the effect of a single long-range (weak effect) is not visible in the beam lifetime. An effect of a compensation effect will not be possible to detect with the available instrumentation.

Therefore, a finite strength in lattice octupoles and a working point close to the 10<sup>th</sup> order resonance was used as shown in Fig. 7. At this modified working point, the beams are marginally stable as the introduction of the single parasitic interaction increases the tune spread of the large amplitude particles on to the 10<sup>th</sup> order resonance, thus enhancing the effect. This setup of marginally stable beams is only used for experiments with single long-range interaction between the two beams. Some relevant lattice and beam parameters are listed in Table 4. The marginally stable beams were essential as the effect of the single long-range interaction on the rather stable RHIC beams is subtle. In one such experiment, the effect on the beam losses on both beams as a function of the separation is shown in Fig. 8. To increase the signal-to-noise ratio the losses are averaged over the 12 bunches.

Note that the Yellow beam was moved while the Blue beam was kept stationary. Therefore, the effect on the Blue beam is of relevance as the losses in the Yellow beam may



Table 3: Summary of long-range beam–beam experiments in RHIC. The wires in the Blue and Yellow ring are named B-BBLR and Y-BBLR respectively. Fields are left blank when the experimental value could not be determined.

fill no	ring	scan	species	rel. $\gamma$	bunches per ring	$Q_x$	$Q_y$	LR location	LR strength (IL) A m	LR separation $d$ $\sigma$	fitted exponent $p$	$d$ for $\tau < 20$ h $\sigma$	comment
...	...	...	...	...	...	...	...	...	...	...	...	...	...
<b>2005</b>													
6981	B	1	p	25.963	1	0.7331	0.7223	IP4	5.3	B moved			weak signal
6981	Y	1	p	25.963	1	0.7267	0.7234	IP4	5.3	B moved			weak signal
6981	B	2	p	25.963	1	0.7351	0.7223	IP4	5.8	B moved			weak signal
6981	Y	2	p	25.963	1	0.7282	0.7233	IP4	5.8	B moved			weak signal
6981	B	3	p	25.963	1	0.7383	0.7247	IR4 DX	8.6	Y moved			weak signal
6981	Y	3	p	25.963	1	0.7271	0.7218	IR4 DX	8.6	Y moved			weak signal
6981	B	4	p	25.963	1	0.7394	0.7271	IR4 DX	8.9	Y moved	4.9	6.5	
6981	Y	4	p	25.963	1	0.7264	0.7388	IR4 DX	8.9	Y moved	2.8		
<b>2006</b>													
7707	B	1	p	106.597	10			IR6 DX	6.7	B moved			weak signal
7707	Y	1	p	106.597	10			IR6 DX	6.7	B moved			weak signal
7707	B	2	p	106.597	10			IR6 DX	6.7	Y moved			weak signal
7707	Y	2	p	106.597	10			IR6 DX	6.7	Y moved			weak signal
7747	B	1	p	106.597	8			IR6 DX	7.9	B moved			weak signal
7747	Y	1	p	106.597	10			IR6 DX	7.9	B moved			weak signal
7747	B	2	p	106.597	8			IR6 DX	7.0	Y moved			weak signal
7747	Y	2	p	106.597	10			IR6 DX	7.0	Y moved			weak signal
7807	B	1	p	106.597	12	0.6912	0.6966	IR6 DX	8.2	Y moved	2.5	3.5	additional octupoles
7807	Y	1	p	106.597	12	0.7092	0.6966	IR6 DX	8.2	Y moved	1.5	3.5	additional octupoles
<b>2007</b>													
8231	B	1	Au	10.520	6	0.2327	0.2141	B-BBLR	12.5	B-BBLR moved	7.2	6.5	
8231	B	1	Au	10.520	6	0.2322	0.2140	B-BBLR	125	B-BBLR moved	7.8	9.0	
8405	B	1	Au	107.369	56	0.2260	0.2270	B-BBLR	125	B-BBLR moved	1.7	15.0	background test
8609	B	1	Au	107.369	23	0.2340	0.2260	B-BBLR	12.5	B-BBLR moved	7.4	6.0	
8609	B	2	Au	107.369	23	0.2340	0.2260	B-BBLR	125	B-BBLR moved	16.0	5.5	
8609	Y	1	Au	107.369	23	0.2280	0.2350	Y-BBLR	12.5	Y-BBLR moved	4.8	9.5	
8609	Y	2	Au	107.369	23	0.2280	0.2350	Y-BBLR	125	Y-BBLR moved	4.1	7.5	
8727	B	1	Au	107.369	23	0.2200	0.2320	B-BBLR	12.5	B-BBLR moved	5.2	9.5	
8727	B	2	Au	107.369	23	0.2200	0.2320	B-BBLR	125	B-BBLR moved	8.1	10.0	
8727	B	1	Au	107.369	23	0.2320	0.2280	Y-BBLR	12.5	Y-BBLR moved	6.3	4.5	
8727	B	2	Au	107.369	23	0.2320	0.2280	Y-BBLR	125	Y-BBLR moved	10.8	5.0	
8727	B	3	Au	107.369	23	0.2320	0.2280	Y-BBLR	125-0	-6.5			ver. chromaticity 2-8
8727	B	4	Au	107.369	23	0.2320	0.2280	Y-BBLR	125	-6.5			ver. chromaticity 8
8727	B	5	Au	107.369	23	0.2320	0.2280	Y-BBLR	125-0	-6.5			
<b>2008</b>													
9664	B	1	d	107.369	12	0.2288	0.2248	B-BBLR	125	B-BBLR moved	3.8	17.0	end of physics store
9664	B	2	d	107.369	12	0.2288	0.2248	B-BBLR	75-125	5.8			end of physics store
<b>2009</b>													
10793	B	-	p	106.597	36	0.691	0.688	B-BBLR	125	B-BBLR moved			with head-on collisions
10793	Y	-	p	106.597	36	0.695	0.692	Y-BBLR	125	Y-BBLR moved			with head-on collisions
10793	B	-	p	106.597	36	0.691	0.688	IR6 DX	12.5	B-BBLR moved			LR compensation
10793	Y	-	p	106.597	36	0.695	0.692	IR6 DX	12.5	Y-BBLR moved			LR compensation

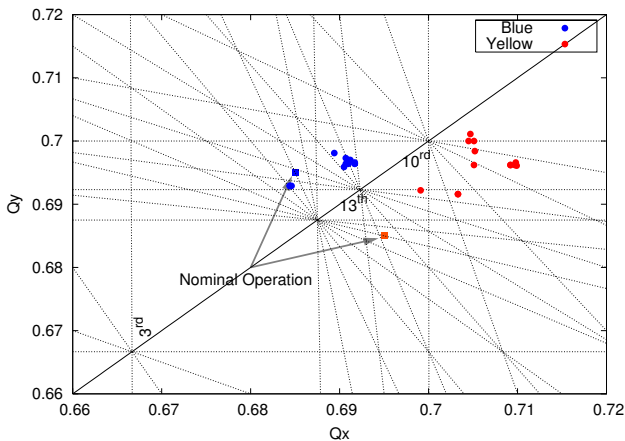


Figure 7: Tunes in the resonance diagram for both beams and both planes during a scan.

also be affected by orbit and tunes shifts. A small effect is visible when the beams are approximately  $5\sigma$  or closer.

Table 4: RHIC parameters for experiments with long-range interactions with proton beams.

Quantity	Enit	Blue	Yellow
Beam energy $E$	GeV/n	100	
Rigidity ( $B\rho$ )	T m	831.8	
Number of bunches	...	12	
LR interaction from IP6	m	10.6	
Norm. Emittances ( $\epsilon_{x,y}$ )	$\mu\text{m}$	15-20	
$\beta_x$ at wire location	m	105	
Tunes ( $Q_{x,y}$ )	...	0.69/0.7	0.71/0.69
$\beta_x$ at wire location	m	1060	342
$\beta_y$ at wire location	m	357	1000
Octupole Strength (kl)	$\text{m}^{-2}$	$6.3 \times 10^{-3}$	

Compensation of such small effects is difficult as the losses are smaller than the natural reproducibility of the machine for a given beam setup. Therefore, it was important to significantly enhance the loss due to the long-range interactions to clearly demonstrate compensation with a DC wire. Increased chromaticity and introduction of head-

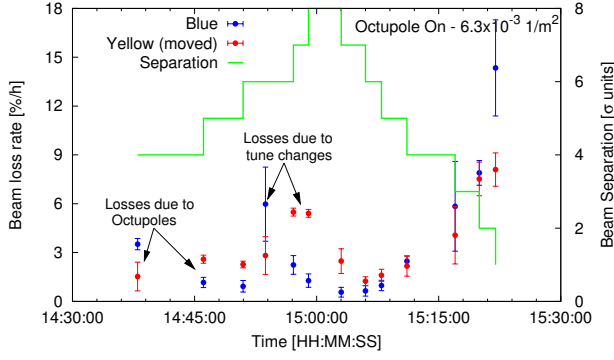


Figure 8: Beam losses due to a single parasitic interaction of the Blue and Yellow beam. The Yellow beam moved closer to the Blue beam from an initially large separation.

on collisions were utilized to enhance the effect of the LR interaction with the DC wires [46].

### Wire Scans on Single Beam

After the installation of the DC wires in 2007, the majority of the experiments were carried out using the individual wires of the Blue and the Yellow ring to characterize the onset of the losses under certain beam conditions [44, 46]. Most of the wire experiments were done with gold beams. Table 5 shows the main beam parameters for the wire experiments at store with gold beams.

Table 5: RHIC parameters for experiments with DC wires on individual gold beams.

Quantity	Unit	Blue	Yellow
Beam energy $E$	GeV/nucleon	100	
Rigidity ( $B\rho$ )	Tm	831.8	
Number of bunches	...	6–56	
Norm. Emittance $\epsilon_{x,y}$	$\mu\text{rad}$	17	17
Distance IP6 to wire centre	m	40.92	
Parameter $K$ (at 50 A)	nm	–30.1	
Hor. tune $Q_x$	...	28.234	28.228
Ver. tune $Q_y$	...	28.226	29.235
$\beta_x$ at wire location	m	1091	350
$\beta_y$ at wire location	m	378	1067

The  $\beta$ -functions in Table 5 are the best estimate of the real  $\beta$ -functions in the machine. The design lattice has  $\beta^* = 0.8$  m at IP6. To calculate the  $\beta$ -functions at the wire location we use  $\beta^* = 0.9$  m, and assume a 10% error. Figure 9 shows the MAD lattice near the interaction region 6 where the wires are located.

The measurements consisted mainly of distance and current scans and simultaneous measurements of the beam loss rate. An overview of the beam losses and wire position for the Blue and the Yellow ring during the course of a scan (Fill 8727) is illustrated in Fig. 10. The beam loss rates are clearly different for the Blue and Yellow beams. This in-

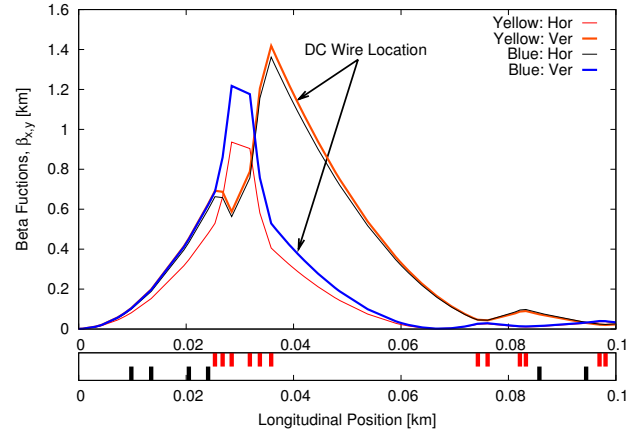


Figure 9: The beta functions from MAD lattice for both rings as a function of longitudinal position.

icates towards different diffusion rates and re-population of tails for the two beams. The exact reason for this difference is not identified. It should be noted that the wire installations are identical.

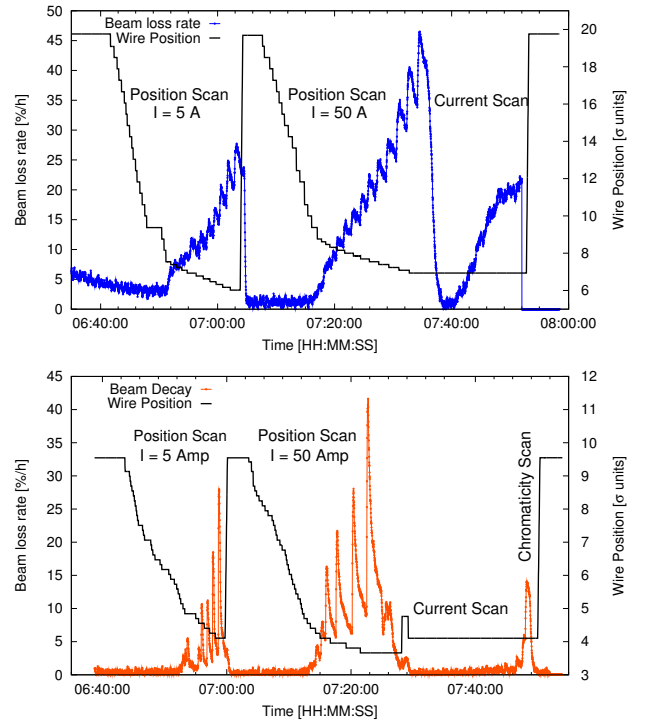


Figure 10: Beam losses and wire position as a function of time during the course of position and current scan (May 2007, Fill 8727).

Orbit, tune and chromaticity changes can be calculated as a function of the long-range strength and distance [47]. These quantities and beam transfer functions are usually recorded to benchmark with theory and simulations. The vertical dipole kick  $\Delta y'$  and vertical tune change  $\Delta Q_y$  due to the wire for a separation  $d$  in the vertical plane between the beam and the wire are given by (assume no horizontal

separation)

$$\Delta y' = \frac{K}{d} \quad \text{and} \quad \Delta Q_{x,y} = \pm \frac{K\beta_{x,y}}{4\pi} \frac{1}{d^2} \quad (8)$$

with

$$K = \frac{\mu_0(IL)}{2\pi(B\rho)}, \quad (9)$$

where  $d$  is the distance between the wire and the beam,  $\mu_0$  the permeability of the vacuum,  $(IL)$  the integrated wire strength, and  $(B\rho)$  the beam rigidity.

Note that we take a positive sign for  $d$  for a wire above the beam, and a negative sign below the beam. We also assume that the reference vertical orbit position at the location of the wire is zero ( $y_{ref} = 0$ ) for the wire current off. The sign of  $K$  depends on the direction of the wire current relative to the beam direction, and the charge of the beam particles. In our case the wire current has the opposite direction to the beam, the Blue wire is above and the Yellow wire below the beam, and the beam particles have positive charges. In this case the sign of  $K$  is negative in Blue, and positive in Yellow. The orbit change  $\Delta y$  at the location of the wire due to the dipole kick  $\Delta y'$ , for  $\Delta y \ll d$ , is then

$$\Delta y = \frac{K\beta_y}{2d} \frac{\cos(\pi Q_y)}{|\sin(\pi Q_y)|}. \quad (10)$$

If the wire comes close to the beam Eq. (10) becomes inaccurate and needs to be replaced by

$$\Delta y = \frac{d}{2} - \sqrt{\frac{d^2}{4} - \frac{1}{2}K\beta_y \cot(\pi Q_y)} \quad (11)$$

where  $d$  is now the distance between the wire and the beam position at zero wire current.

Orbit and tune changes agree with expectations under well controlled experimental circumstances [46, 48]. Figure 11 shows a comparison of the measured beam trajectories to the analytical prediction as a function of the separation between the wire and the Blue beam.

Figure 12 shows a comparison of the measured tunes to the analytical prediction as a function of the separation between the wire and the beam.

The beam lifetime, however, is determined through the nonlinear beam-beam effect and can only be assessed in detailed simulations. Figure 13 (top) shows the beam loss rate as a function of the vertical wire distance to the beam. The onset of losses due to a long-range type interaction between the wire and the beam is visible. Similarly the effect on beam losses due to a current scan at a fixed distance is shown in Fig. 13 (bottom). The approximate separation in the Blue ring is  $9\sigma$  and in the Yellow ring is  $5\sigma$ . The Yellow ring shows very weak or no effect with a current scan which is probably due to a previous distance scan resulting in a cleaning of the large amplitude particles.

It was speculated that the beam lifetime  $\tau$  can be expressed as  $\tau = Ad^p$  where  $A$  is an amplitude,  $d$  the distance between wire and beam, and  $p$  an exponent that would typically be in a narrow range. For the SPS  $p$  had been found to

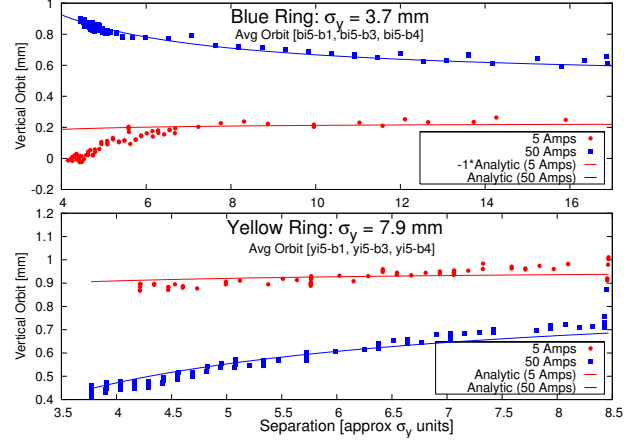


Figure 11: Vertical orbit change (average of 3 BPMs near wire) as a function of vertical distance, in Blue and Yellow ring at 5 A and 50 A. Solid lines in all plots represent the analytical prediction.

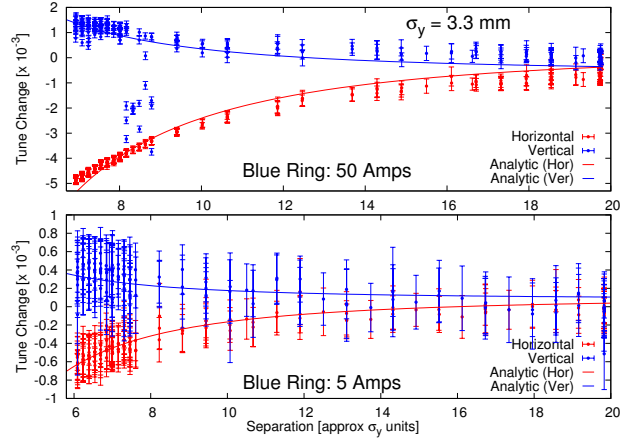


Figure 12: Horizontal and vertical tune change for 50 A and 5 A wire current, for the Blue ring. Solid lines in all plots represent the analytical prediction.

be about 5, and for the Tevatron to be about 3 [49]. In Table 3 the fitted exponents are listed for all cases for which a fit was possible. The fitted exponents range from 1.7 to 16, i.e.  $p$  is not constrained within a narrow range. Ten of the thirteen  $p$  values are between 4 and 10. Figure 14 shows the fitted exponents  $p$  as a function of the ion tunes in the upper part, and the proton tunes in the lower part. Ion tunes near the diagonal and away from either horizontal or vertical resonances show smaller exponents  $p$ . The experiments also showed that the beam lifetime is reduced with increased chromaticity [46].

Another simple measure of assessing the long-range beam-beam effect in experiments is the distance between the beam and wire (or other beam) at which the beam lifetime becomes smaller than a certain value. We have chosen this value to be 20 h, which would imply a luminosity lifetime of 10 h or less. Table 3 shows an amplitude range between 3.5 and 17  $\sigma$ . With the available amount of data

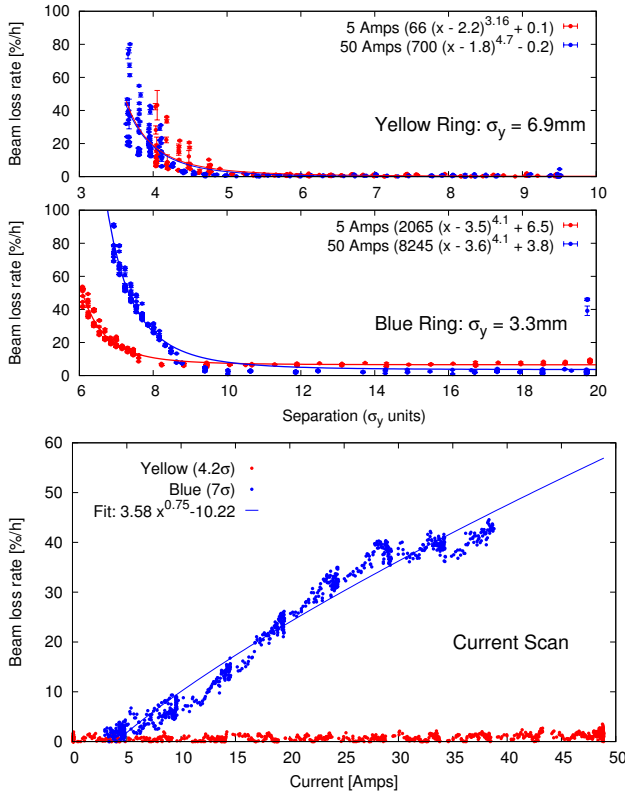


Figure 13: Top: Beam loss as a function of the DC wire separation to the Blue and the Yellow beams at 5 A and 50 A. Bottom: Beam loss due to a current scan in the DC wire fixed at a given distance from the beam. Solid lines in all plots show a power law fit to the losses.

no clear correlation can be established between this distance and the fitted coefficient  $p$ . In two cases the distance was found to be as large as or larger than  $10 \sigma$ , and most cases fall between 4 and  $10 \sigma$ . Operation with less than  $5 \sigma$  separation appears to be difficult [50]. Note that the beam is sometimes used for multiple scans and that a large lifetime drop at large distances is more typical for previously unused beams (Table 3).

One important goal of the experiments is to benchmark simulations. In several simulations the onset of large losses as a function of the distance between wire and beam was reproduced within about  $1 \sigma$  [30, 48, 51–55]. One such comparison is shown in Fig. 15.

### Long-range Effects with Head-on Collisions

End of physics fills were initially used to test the effect of the wires on colliding gold and deuteron beams (see Table 3). It should be noted that the beam–beam parameter of proton beams in RHIC is approximately three times larger than the beam–beam parameter of heavy ion beams. The first dedicated experiment with protons to compare the effect of the wire on colliding beams and compensation of a single LR beam–beam interaction was conducted in 2009 at 100 GeV. Due to aperture considerations for decreasing  $\beta^*$ ,

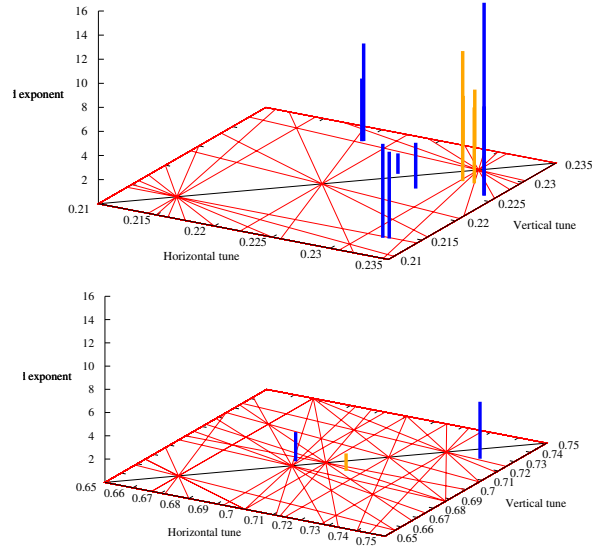


Figure 14: Fitted exponents  $p$  for long-range beam–beam experiments as a function of the ion tunes (top) and the proton tunes (bottom). The fitted exponents range from 1.7 to 16.

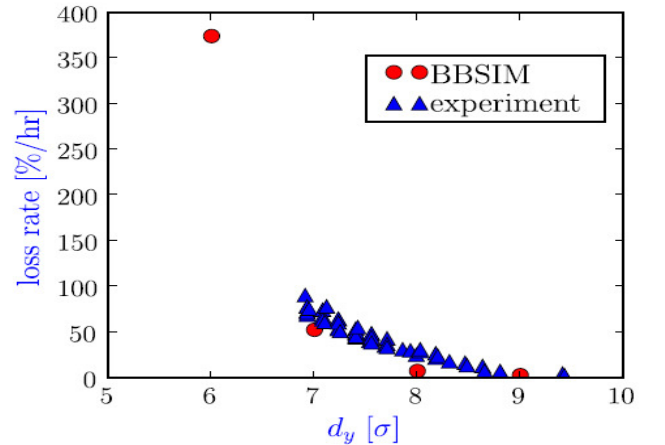


Figure 15: Comparison of measured and simulated beam loss rate as a function of distance between wire and beam. Experiment with gold beam at store, wire strength of 125 Am [51, 53].

the Blue wire was removed during the shutdown after the 2009 run and the Yellow wire was removed subsequently. Therefore, the experiments in 2009 serve as the final set of measurements for LR beam–beam with RHIC as a test bed. The relevant RHIC beam and lattice parameters are listed in Table 6 for the experiments in 2009.

Prior to a long-range compensation attempt, a position scan of the wire on each beam was performed with a wire current of 50 A. A  $36 \times 36$  bunch pattern with six non-colliding bunches was chosen to enable a comparison of the lifetime in the presence of the wire between single beam



Table 6: Relevant RHIC beam and lattice parameters for experiments with proton beams.

Quantity	Unit	Blue	Yellow
Beam energy $E$	GeV	100	
Rigidity ( $B\rho$ )	Tm	333.5	
Number of bunches	-	36	
# of colliding bunches	-	30	
Bunch intensity	$10^{11}$	1.7	1.7
Norm. Emittance $\epsilon_{x,y}$	$\mu\text{rad}$	25,24	49,19
Horizontal tune $Q_x$	...	28.691	28.232
Vertical tune $Q_y$	...	29.688	29.692
Chromaticities ( $\xi_x, \xi_y$ )	...	(+2, +2)	
$\beta_x$ at wire location	m	1566	556
$\beta_y$ at wire location	m	576	1607

and colliding beams simultaneously. The corresponding beam loss rates as a function of beam to wire separation on both colliding and non-colliding bunches were measured. The initial beam loss rates with colliding beams were stabilized to the nominal 10% per hour. The maximum total beam losses for the wire movements towards the beam at fixed current were constrained to 100–150% per hour for a very short period to avoid disrupting the beam quality significantly for subsequent measurements.

Figure 17 shows the evolution of the intensity between bunches with and without head-on collisions. It is evident that the bunches with the head-on collisions have a more severe effect from the LR forces of the wire. Several hypotheses can be formulated to explain the increased losses for bunches with head-on collision.

- The dynamic aperture for the bunches with head-on is significantly smaller than that of the single beam which could lead to the observed beam losses.
- It was also suggested by an anonymous referee that the addition of the head-on collisions enhances the diffusion leading to enhanced losses in the presence of long-range interactions. Figure 17 clearly shows a larger initial slope for bunch intensities with collisions. However, it is difficult to untangle the contribution from the reduced dynamic aperture as opposed to enhanced diffusion.
- The additional tune shift due to the wire along with large head-on tune shift could lead to beam losses due to very limited tune space available. No tune optimization was performed during the experiment.
- The effect of the wire on the orbit can introduce a static offset between the two beams at the IP which is approximately proportional to the wire distance. A large offset due to the kick from the wire can lead to emittance blow-up and beam losses [31]. The relative offset at the collision point during the wire scan with 50 A (see Fig. 16) is well below the  $1\sigma$  level which is very small.

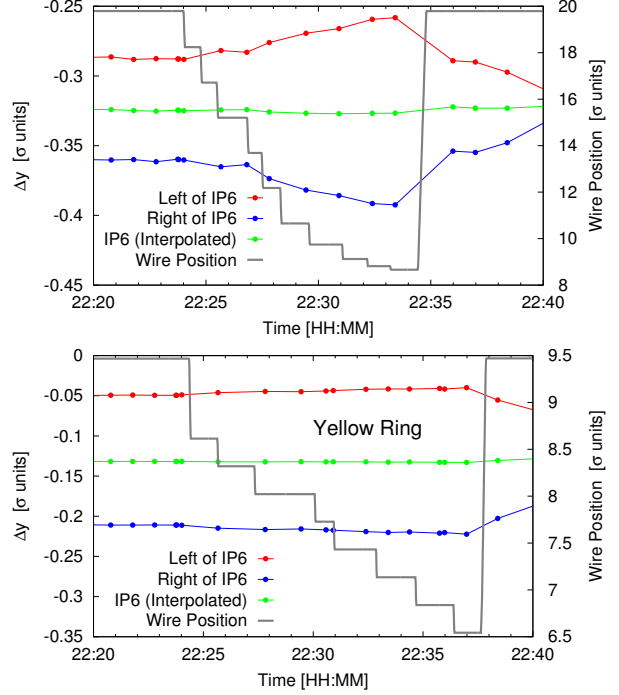


Figure 16: Orbit offset at IP6 as a function of the wire position for Blue (top) and Yellow (bottom) rings with a current of 50 A.

However, simulations to support each of the above hypotheses to explain its contribution towards observed losses is beyond the scope of this paper.

### Single Long-range and Wire Compensation

The bunch spacing and the interaction region geometry in RHIC does not inherently have LR beam–beam interactions. It is therefore necessary to shift the collision point towards the DX magnet closest to the DC wires as noted before. This location enables an artificially induced LR interaction between the two beams and simultaneously allows for a minimum phase advance between the LR interaction and DC wires (6 deg). Additionally, this location has sufficient aperture for an orbit scan with the range of interest ( $3\text{--}10\sigma$ ). Figure 18 shows the trajectories of the Blue and Yellow rings with the LR interaction set at approximately  $3.1\sigma$ .

The individual bunch intensities and beam losses were recorded during the position scan with the LR compensation [56]. Figure 19 shows the beam losses as a function of the wire position. In the Blue ring, the losses are always increasing as the wire approaches the beam. Therefore, no evidence of compensation of the LR interaction from the Blue beam is visible. However, in the Yellow ring, the beam lifetime improved as the beam to wire distance approaches  $3\sigma$  (Fig. 19). Consecutive retractions and restoration of the beam to wire distance to  $3\sigma$  show similar improvement of the beam lifetime. This indicates a compensation of the effect of LR interaction by the DC wire.

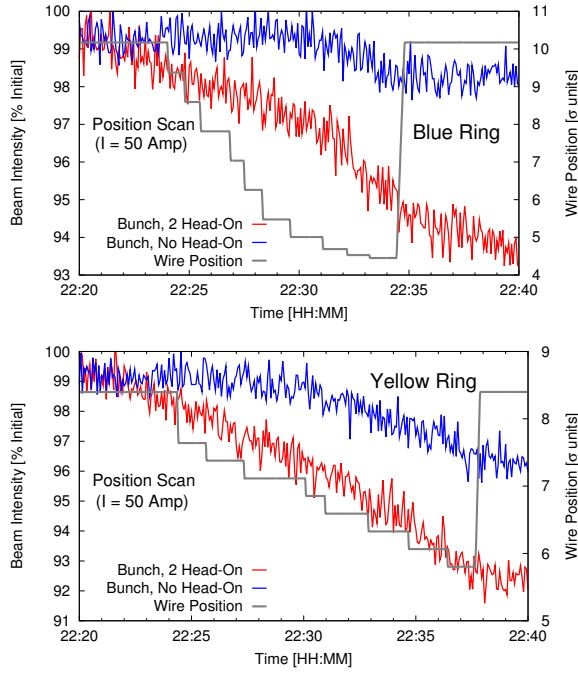


Figure 17: Single bunch intensities as a function of wire position for Blue (top) and Yellow (bottom) rings with a current of 50 A. Comparison between bunches with head-on and no head-on collision is shown.

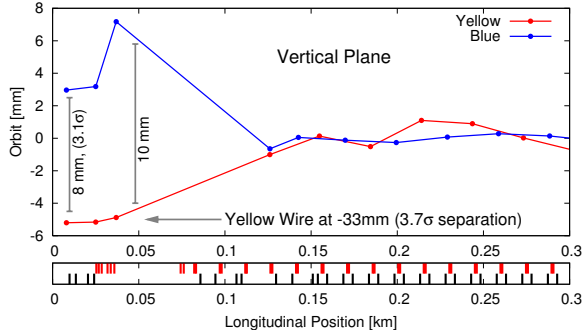


Figure 18: Orbits right of IP6 for the Blue and the Yellow ring with the LR interaction setup near the DX magnet at approximately  $3.1 \sigma$ .

In addition to beam losses, the individual bunch intensities with and without LR interactions and simultaneous compensation is shown in Fig. 20. Note that all 36 bunches experience the effect of the DC wire, but only 30 bunches experience LR interactions. Therefore, only bunches with an LR interaction can experience a compensation. In the Blue ring, the bunch intensity evolution is similar for bunches with and without LR compensation. Hence, only the effect from the wire is visible. The bunches with LR interaction and simultaneous compensation have reduced beam losses as compared to the bunches that only see the wire. This is consistent with the beam loss measurements (Fig. 19).

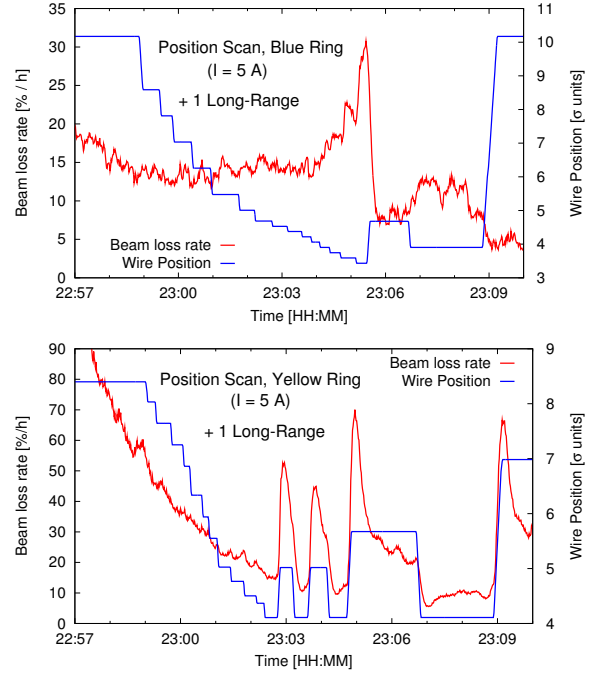


Figure 19: Beam loss rate for a Blue (top) and Yellow (bottom) bunch with one long-range interaction, and an additional wire interaction. The wire position varies, and the wire current is constant at 5 A.

## SUMMARY

Long-range beam-beam experiments were conducted in RHIC from 2005 to 2009. The motivation for these were two-fold. First, the experimental data can benchmark simulation codes for situations of strong localized long-range beam-beam interactions as they will exist in the LHC. Second, the compensation of a single long-range beam-beam interaction can be tested in a scheme that is also usable in the LHC.

These experiments complement the experience with long-range beam-beam interactions in the Sp̄pS and Tevatron, wire experiments in the SPS, and the partial long-range compensation in DAΦNE. The RHIC wires created strong localized long-range beam-beam effects, comparable in strength to the effect expected in the LHC, with a beam that has a lifetime typical of hadron colliders, and including head-on beam-beam collisions. The observed orbit and tune changes due to the wire were as expected. The effect of the long-range beam-beam interactions on the beam loss rate is sensitive to a number of beam parameters such as the tunes and chromaticities. Fitting the beam lifetime  $\tau$  to an exponential function  $\tau \propto d^p$  as a function of the distance  $d$  between the beam and the wire, exponents  $p$  in the range between 1.7 and 16 were found. Distances smaller than  $5 \sigma$  created losses too large for collider operation. The experimentally observed distance from the wire to the beam at which large beam losses set in could be reproduced in simulations within  $1 \sigma$ . The beam lifetime with long-range interactions created by the wire was de-

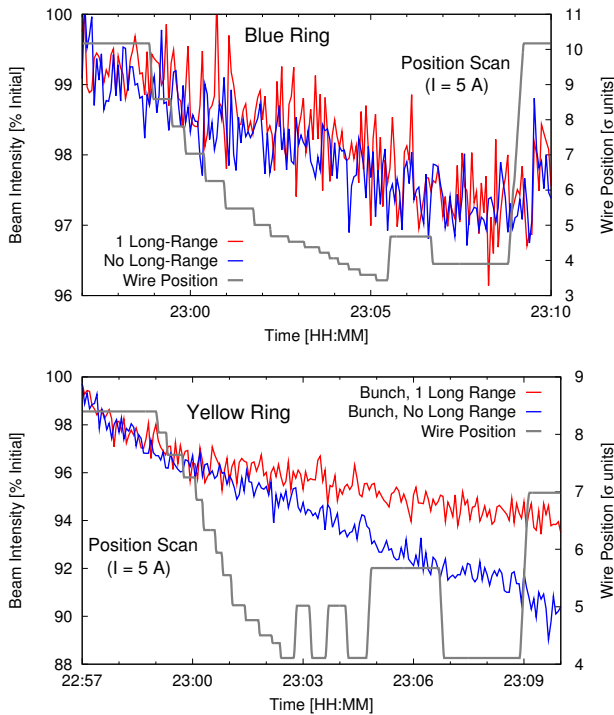


Figure 20: Beam intensity comparison between bunches with a single long-range and no long-range interaction as a function of the wire position for Blue (top) and Yellow (bottom) rings with a wire current of 5 A.

graded further through head-on collisions. A single attempt to compensate long-range beam–beam interaction via a DC wire showed evidence of compensation.

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